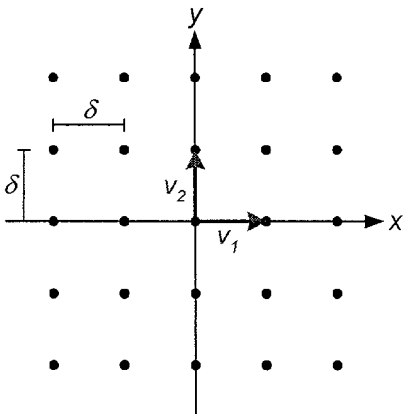


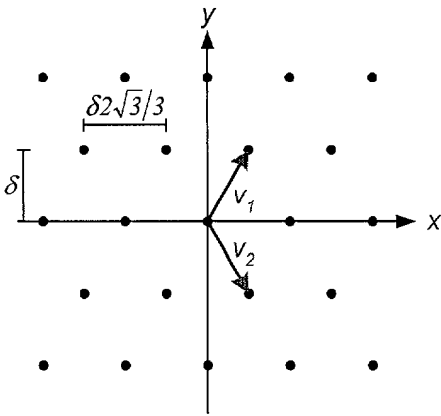
100

| Map name                                    | Sampling Requirement | Minimum Isotropy | Map Components |
|---|----------------------|------------------|----------------|
| OpenGL                                      | $\infty$             | 0                | 1              |
| Cube  | 24                   | 0.58             | 6              |
| Dual Stereographic                          | 32                   | 1                | 2              |
| Lat/Long                                    | 19.7                 | 0                | 1              |
| Dual Equidistant*                           | 19.7                 | 0.64             | 2              |
| Low Distortion Area Preserving*             | 19.7                 | 0.29             | 1              |
| Polar-Capped* (stretch invariant)           | 14.8                 | 0.71             | 3              |
| Polar-Capped* (conformal)                   | 16.5                 | 1                | 3              |
| Polar-Capped* (hexagonally reparameterized) | 13.5                 | 0.58             | 3              |
| Optimal Isometric**                         | 12.57                | 1                | $\infty$       |
| Optimal**                                   | 10.9                 | 0.58             | $\infty$       |

Fig. 2

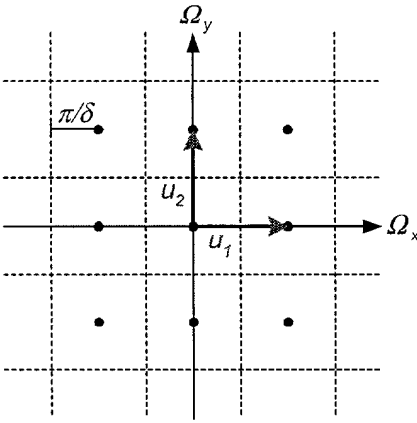


(a) rectangular

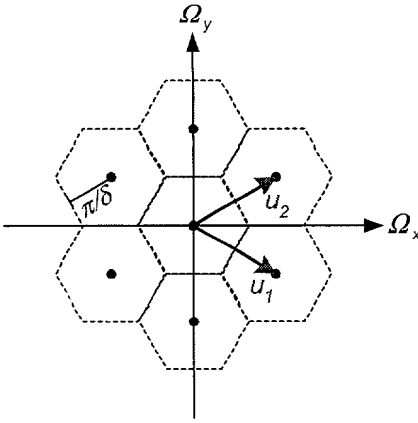


(b) hexagonal

Fig. 3



(a) rectangular



(b) hexagonal

Fig. 4

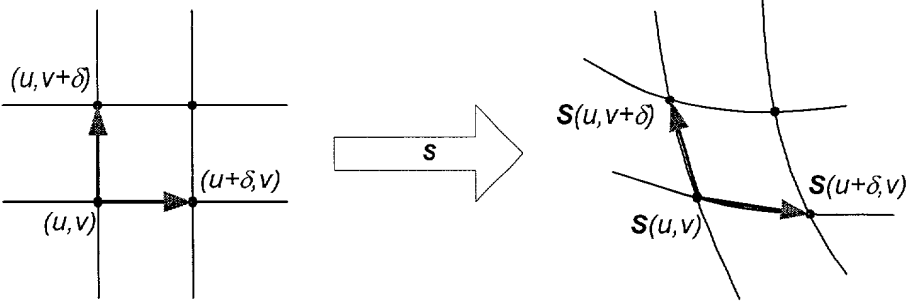
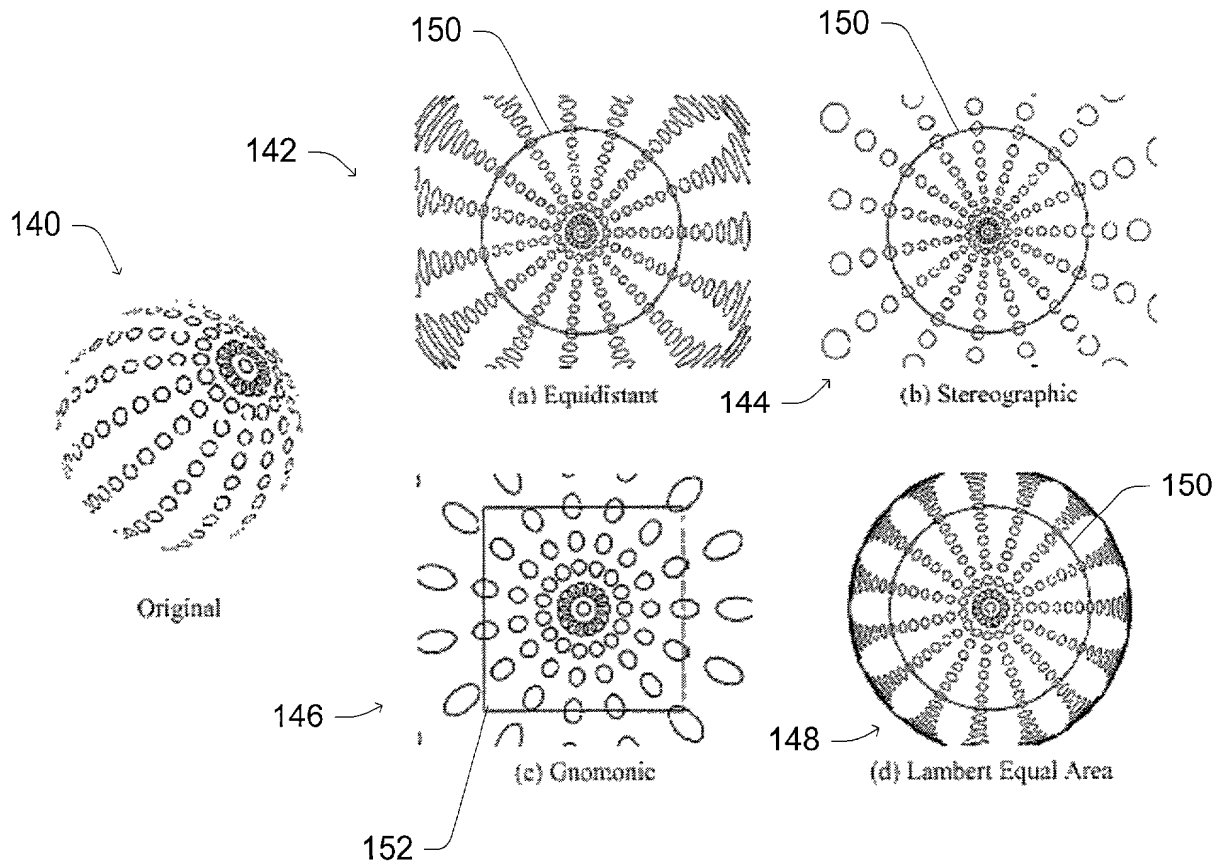


Fig. 5

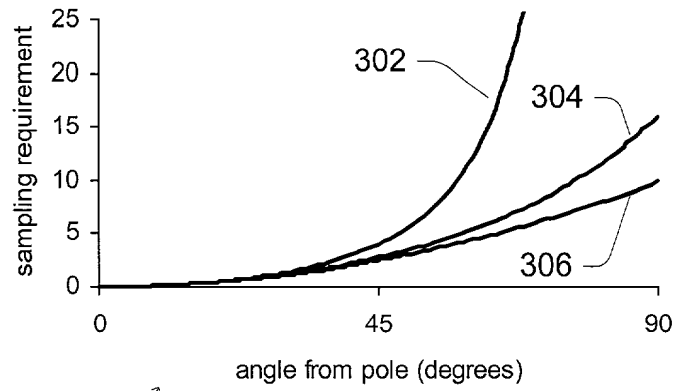


*Fig. 6*

200

|                           | Equidistant   | Gnomonic                                 | Stereographic                           | Lambert<br>Equal Area                    |
|---------------------------|---|--|---|--|
| $\theta(r)$               | $(\pi/2)r$  | $\cos^{-1}\left(\sqrt{1/(r^2+1)}\right)$ | $\cos^{-1}\left((1-r^2)/(1+r^2)\right)$ | $\cos^{-1}(1-r^2)$                       |
| properties                | stretch-preserving  | projects great circles to lines          | conformal, projects circles to circles  | area-preserving                          |
| $r^*$ covering hemisphere | $[0, 1]$  | $[0, \infty]$                            | $[0, 1]$                                | $[0, 1]$                                 |
| $r^*$ covering sphere     | $[0, 2]$  | —  | $[0, \infty]$                           | $[0, \sqrt{2}]$                          |
| $r(\theta)$               | $2\theta/\pi$   | $\tan \theta$                            | $\tan(\theta/2)$                        | $\sqrt{1-\cos \theta}$                   |
| $\sin \theta$             | $\sin((\pi/2)r)$  | $r/\sqrt{r^2+1}$                         | $2r/(1+r^2)$                            | $r\sqrt{2-r^2}$                          |
| $\cos \theta$             | $\cos((\pi/2)r)$  | $\sqrt{1/(r^2+1)}$                       | $(1-r^2)/(1+r^2)$                       | $1-r^2$                                  |
| $\lambda_1(\theta)$       | $\pi/2$   | $\cos \theta$                            | $1+\cos \theta$                         | $2/\sqrt{1+\cos \theta}$                 |
| $\lambda_2(\theta)$       | $(\pi/2)\text{sinc } \theta$                                    | $\cos^2 \theta$                          | $1+\cos \theta$                         | $\sqrt{1+\cos \theta}$                   |
| $\alpha(\theta)$          | $\text{sinc } \theta$   | $\cos \theta$                            | 1                                       | $(1+\cos \theta)/2$                      |
| $\tau(\theta)$            | $(\pi/2)^2 \text{sinc } \theta$                                 | $\cos^3 \theta$                          | $(1+\cos \theta)^2$                     | 2  |
| $\lambda_1^*(\theta)$     | $\pi/2$   | 1  | 2                                       | $2/\sqrt{1+\cos \theta}$                 |
| $M_s(\theta)$             | $4\theta^2$   | $4 \tan^2 \theta$                        | $16 \tan^2(\theta/2)$                   | $16 \tan^2(\theta/2)$                    |
| inverse map               | $f = (\pi/2)\text{sinc}(\cos^{-1} z)$<br>$u = x/f$<br>$v = y/f$ | $u = x/z$<br>$v = y/z$                   | $u = x/(1+z)$<br>$v = y/(1+z)$          | $u = x/\sqrt{1+z}$<br>$v = y/\sqrt{1+z}$ |

Fig. 7



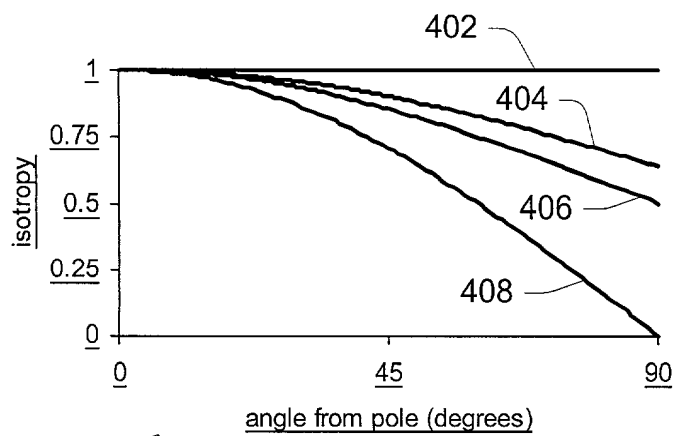
300

Fig. 8

| Solid        | $M_s$ | $\alpha^*$ | Components |
|--------------|-------|------------|------------|
| tetrahedron  | 41.57 | 0.33       | 4          |
| cube         | 24    | 0.58       | 6          |
| octahedron   | 20.78 | 0.58       | 8          |
| dodecahedron | 16.65 | 0.79       | 12         |
| icosahedron  | 15.16 | 0.79       | 20         |

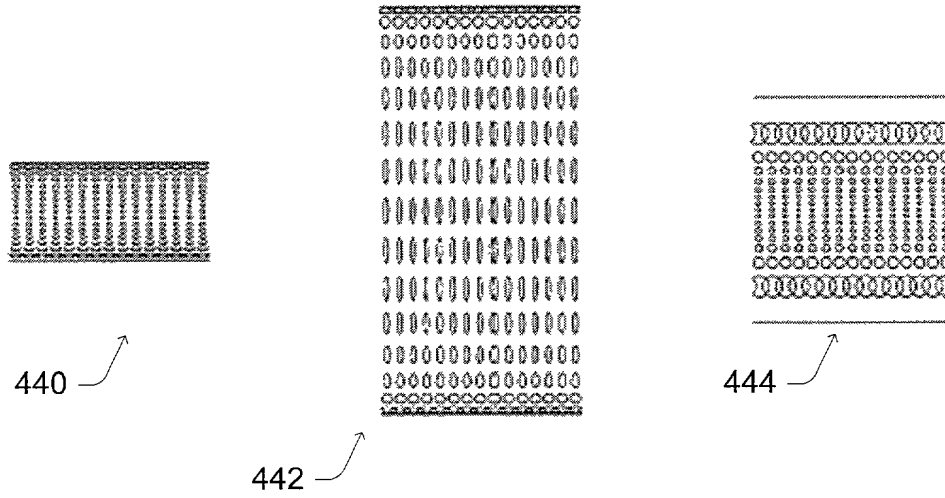
320

Fig. 9



400

Fig. 10



*Fig. 11*

500

|                       | Plane Chart  | Equal Area  | Mercator   |
|-----------------------|--|---|--|
| $\theta(v)$           | $2\pi v$   | $\sin^{-1} v$   | $\sin^{-1}(\tanh(2\pi v))$   |
| properties            | stretch-preserving   | area-preserving                                       | conformal  |
| $v$ covering sphere   | $[-1/4, 1/4]$  | $[-1, 1]$   | $[-\infty, \infty]$  |
| $v(\theta)$           | $\theta/(2\pi)$  | $\sin \theta$   | $\tanh^{-1}(\sin \theta)/(2\pi)$<br>$= \ln((1 + \sin \theta)/(1 - \sin \theta))/(2\pi)$                    |
| $\cos \theta$         | $\cos(2\pi v)$   | $\sqrt{1 - v^2}$                                      | $\operatorname{sech}(2\pi v)$<br>$= 2/(e^{-2\pi v} + e^{2\pi v})$  |
| $\sin \theta$         | $\sin(2\pi v)$   | $v$   | $\tanh(2\pi v)$<br>$= (e^{2\pi v} - e^{-2\pi v})/(e^{2\pi v} + e^{-2\pi v})$                               |
| $\lambda_1(\theta)$   | $2\pi$   | $\max(1/\cos \theta, 2\pi \cos \theta)$               | $2\pi \cos \theta$   |
| $\lambda_2(\theta)$   | $2\pi \cos \theta$   | $\min(1/\cos \theta, 2\pi \cos \theta)$               | $2\pi \cos \theta$   |
| $\alpha(\theta)$      | $\cos \theta$  | $\min(1/(2\pi \cos^2 \theta), 2\pi \cos^2 \theta)$    | 1  |
| $\tau(\theta)$        | $4\pi^2 \cos \theta$   | $2\pi$  | $4\pi^2 \cos^2 \theta$   |
| $\lambda_1^*(\theta)$ | $2\pi$   | $\max(1/\cos \theta, 2\pi)$                           | $2\pi$   |
| $M_s(\theta)$         | $2\pi \theta$  | $\max(1/\cos^2 \theta, 4\pi^2) \sin \theta$           | $2\pi \tanh^{-1}(\sin \theta)$<br>$= \pi \ln((1 + \sin \theta)/(1 - \sin \theta))$                         |
| inverse map           | $u = (\operatorname{atan} 2(y, x))/(2\pi)$<br>$v = (\sin^{-1} z)/(2\pi)$ | $u = (\operatorname{atan} 2(y, x))/(2\pi)$<br>$v = z$ | $u = (\operatorname{atan} 2(y, x))/(2\pi)$<br>$v = \tanh^{-1} z/(2\pi)$<br>$= \ln((1 + z)/(1 - z))/(4\pi)$ |

Fig. 12



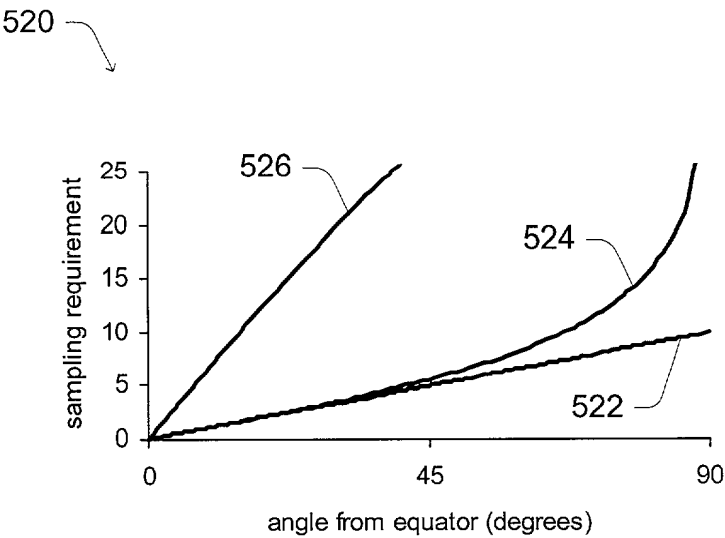


Fig. 13

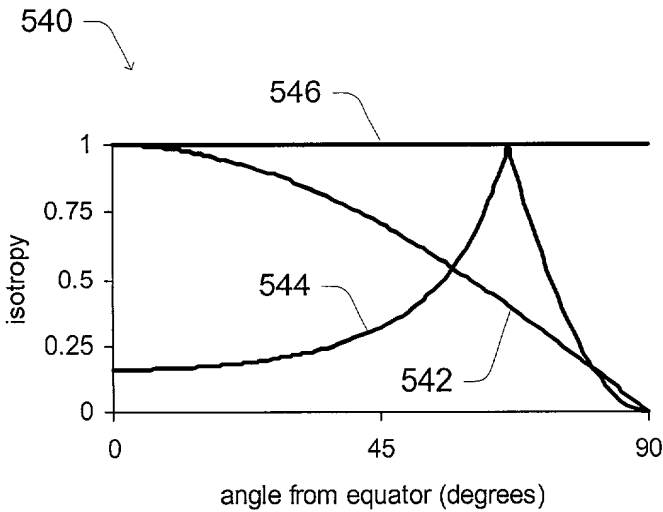
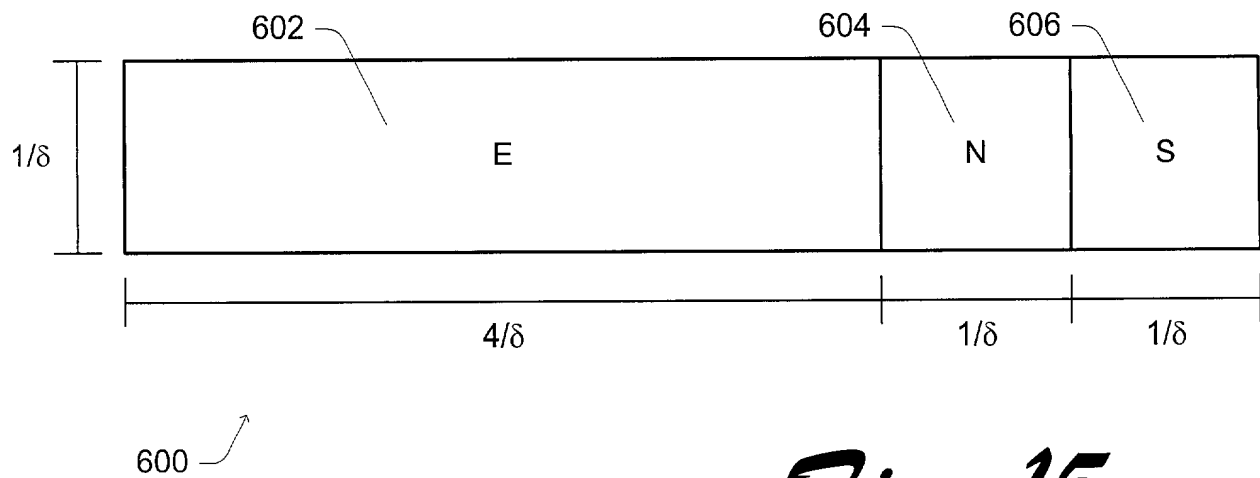
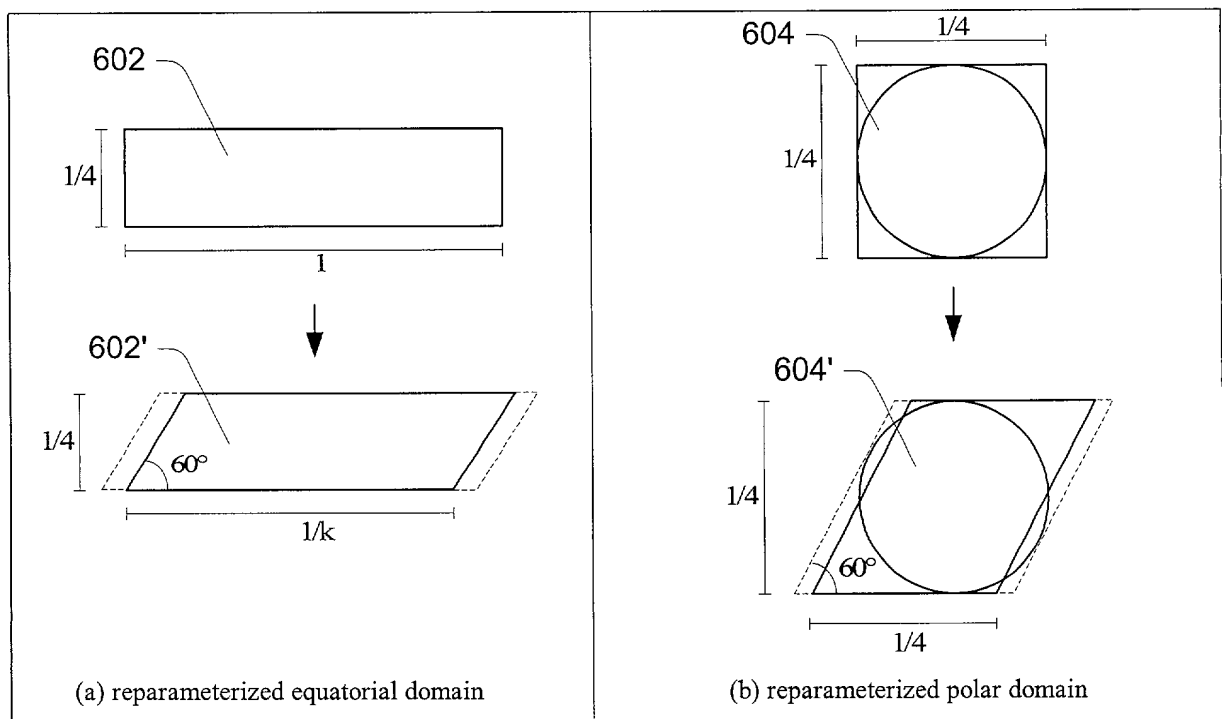


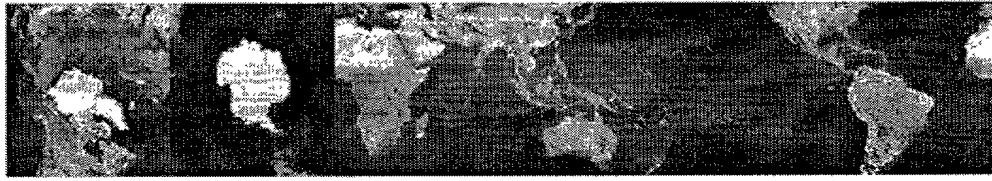
Fig. 14



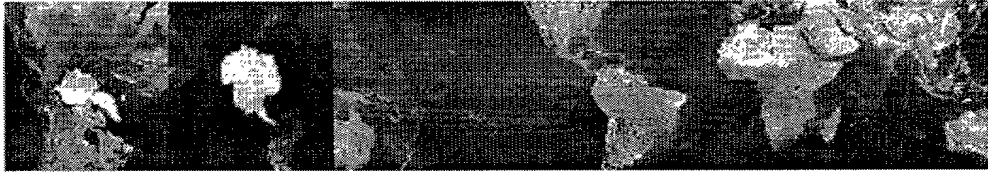
*Fig. 15*



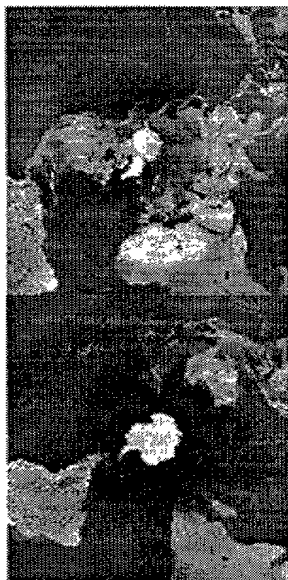
*Fig. 16*



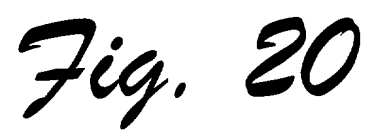
*Fig. 17*

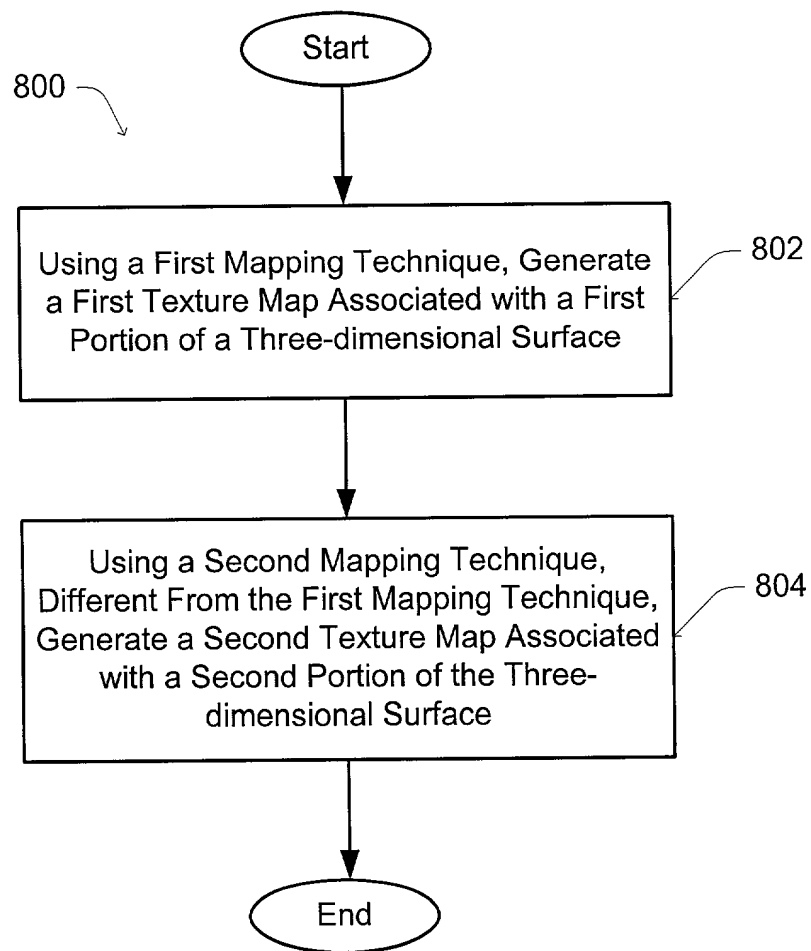


*Fig. 18*



*Fig. 19*



*Fig. 23*